

1- $f(x) = \begin{cases} -\pi & 0 < x < \pi \\ (x-\pi) & \pi < x < 2\pi \end{cases}$ and $f(x + 2\pi) = f(x)$. Fourier series of $f(x)$ is represented by

$$\frac{a_0}{2} + \sum (a_n \cos nx + b_n \sin nx) \text{ then } a_0 \text{ is}$$

A- $\frac{3\pi}{2}$

B- $\frac{\pi}{2}$

C- $-\frac{\pi}{2}$

D- π

2- $f(x) = \begin{cases} 0 & -5 < x < 0 \\ 3 & 0 < x < 5 \end{cases}$, period 10 and Fourier series of $f(x)$ is represented by

$$\frac{a_0}{2} + \sum (a_n \cos \frac{n\pi x}{l} + b_n \sin \frac{n\pi x}{l}) \text{ then } a_0 \text{ is}$$

A- (1)

B- (5)

C- (4)

D- (3)

3- According to problem (2), b_n is

A- $\frac{3(1 + \cos n\pi)}{n\pi}$

B- $\frac{3(1 - \cos n\pi)}{n\pi}$

C- $\frac{3(1 - \sin n\pi)}{n\pi}$

D- $\frac{3(1 + \sin n\pi)}{n\pi}$

4- According to problem (2), a_n is

A- (0)

B- (1)

C- (2)

D- (3)

5- $f(x) = \begin{cases} 0 & -\pi < x < 0 \\ \cos x & 0 < x < \pi \end{cases}$ and $f(x + 2\pi) = f(x)$. Fourier series of $f(x)$ is represented by

$$\frac{a_0}{2} + \sum (a_n \cos nx + b_n \sin nx) \text{ then } b_1 \text{ is}$$

A- (-1)

B- (1)

C- (0)

D- (2)

6- The Fourier series of an odd periodic function, contains only

A- odd harmonics

B- even harmonics

C- cosine terms

D- sine terms

7- The Fourier Transform of $f(x) = \begin{cases} 1, & |x| < 1 \\ 0, & |x| > 1 \end{cases}$ is

A- $\sqrt{\frac{2}{\pi}} \frac{\cos(\alpha)}{\alpha}$

B- $\sqrt{\frac{2}{\pi}} \frac{\sin(\alpha)}{\alpha}$

C- $\sqrt{\frac{1}{\pi}} \frac{\cos(\alpha)}{\alpha}$

D- $\sqrt{\frac{1}{\pi}} \frac{\sin(\alpha)}{\alpha}$

8- A "periodic function" is given by a function which

A- has a period $T=2\pi$,

C- satisfies $f(t+T) = t$,

B- satisfies $f(t+T) = -t$,

D- has a period $T=2\pi$

9- The constant function is

A- an odd function

C. an even function

B- neither even nor odd

D. none of these

10- If $f(x)$ is an even function, then its graph is symmetric about

A- y - axis,

B- x - axis,

C- opposite quadrants,

D- none of these

with my best wishes, Prof. Dr. Khaled S.A. Hassaneen